NPS ARCHIVE 1966 PRATHER, R.

INVESTIGATION OF THE ULTRASONIC DYNAMIC VISCOELASTIC PROPERTIES OF AQUEOUS POLYETHYLENE OXIDE SOLUTIONS

ROBERT JAMES PRATI-IER, JR.

LIBRARY NAVAL POSTGRADUATE SCHOOL MONTEREY, CALIF. 93940 DUDLEY KNOX LIBRARY
NAVAL POSTGRADUATE SCHOOL
MONTEREY, CA 93943-5101





INVESTIGATION OF THE ULTRASONIC
DYNAMIC VISCOELASTIC PROPERTIES

OF AQUEOUS POLYETHYLENE OXIDE

SOLUTIONS

by

Robert James Prather, Jr.
Lieutenant, United States Navy
B.S., United States Naval Academy, 1958



Submitted in partial fulfillment for the degree of

MASTER OF SCIENCE IN PHYSICS

from the

UNITED STATES NAVAL POSTGRADUATE SCHOOL May 1966

NPSARCHIVE 1966 PLATHER, R.

ABSTRACT

Some of the viscoelastic properties of aqueous solutions of polyethylene oxide were studied using the method of pulsed torsional wave propagation in the ultrasonic frequency range. Measurements of the changes in attenuation and phase of the wave train in a rod when the rod is immersed in the solutions permit calculation of the components of the complex shear modulus (or the complex viscosity). The results from this study are combined with those of others at different frequencies to obtain a measure of the variation of the viscoelastic properties over a wide frequency range. This can be interpreted qualitatively in terms of a distribution of relaxations at low frequencies corresponding to the configurational relaxation of the molecule as a whole and a relaxation frequency of approximately 40 kHz corresponding to that of the shortest chain segment. The real part of the complex viscosity approaches a value at high frequencies, dependent upon the concentration, which is greater than that of water thus showing the existance of a "local viscosity" which is dependent upon concentration.

# DUDLEY KNOX LIBRARY NAVAL POSTGRADUATE SCHOOL MONTEREY, CA 93943-5101

# TABLE OF CONTENTS

Section		Page
1.	Introduction	5
2.	Theory of Measurement	6
3.	Measurements	9
4.	Equipment and Procedures	11
5.	Results	15
6.	Discussion of Error	16
7.	Acknowledgements	16
8.	Tables	17
9.	Figures	18
10.	Bibliography	27

# TOTAL CATERNAL LIST OF ILLUSTRATIONS

The Particular Inc.

Figure		Page
1.	Block Diagram Showing Experimental Setup for Measurements Using Traveling Torsional Waves	18
2.	Barium Titanate Crystal Electrode Location	19
3.	The Resistive and Reactive Loading for 0.25 Percent Polyethylene Oxide Solution as a Function of Frequency	20
4.	The Resistive and Reactive Loading for 0.50 Percent Polyethylene Oxide Solution as a Function of Frequency	21
5.	The Resistive and Reactive Loading for 1.0 Percent Polyethylene Oxide Solution as a Function of Frequency	22
6.	The Real Component of the Complex Shear Modulus as a Function of Frequency and Concentration	23
7.	The Imaginary Component of the Complex Shear Modulus as a Function of Frequency and Concentration	24
8.	The Real Component of the Complex Shear Modulus as a Function of Frequency and Concentration	25
9.	The Real Component of the Complex Viscosity as a Function of Frequency and Concentration	26

#### 1. Introduction

Solutions of polyethylene oxide display both viscous and elastic behavior when subjected to a shearing stress thus they belong to the class of fluids called viscoelastic. The solutions also show a "non-Newtonian" viscous property called "pseudoplasticity", which is the designation given fluids that demonstrate an apparent decrease in viscosity with increasing rates of shear (1,15).

Polyethylene oxide is known to form very long linear chains in aqueous solutions and has the molecular structure  $(-CH_2-CH_2-0-)_n$ . The resin used to make the solutions was produced by the Unior Carbide Company and has the trade name POLYOX-301. This polymer has an average molecular weight of about 4,000,000 (14). Henceforth in this paper the term polyox will be used vice polyethylene oxide when referring to this product.

Polyox, being a very long chain molecule, is flexible and can take up many different shapes. Since certain coiled shapes are more probably than others, the molecule will tend to return to those shapes if the stress is removed (7). This type of elasticity is called configurational elasticity, and the rate with which it regains the most probably shape after a deformation determines the relaxational time for such configurational elasticities.

Previous research at this institution (1,4) and at the University of Wisconsin (16) show that at frequencies in the mHz range the viscous effects of the polymer chains were relaxed while at frequencies in the range of 0.1-100 Hz the relaxation processes were present and must also be occurring at both higher and lower frequencies. Since this could not be explained in terms of the simple Maxwellian element

with a single relaxation frequency, this investigation was conducted at frequencies in the range of 20-70 kHz in order to obtain a measure of the distribution of relaxation frequencies.

## 2. Theory of Measurement

In order to investigate the viscoelastic properties of polyox solutions in the frequency range of 20-70 kilohertz, the method of pulsed torsional wave propagation was chosen (11). Piezoelectric torsional transducers cemented to a metal rod were used to send a train of torsional waves down the rod and to receive echos from the free end. The effects of the fluid in contact with the surface of the rod on the attenuation and phase of the wave were observed.

The solution of the Navier-Stokes equation for parallel oscillatory flow near a flat plate is given (13) as

where y is the direction of motion and z is the direction perpendicular to the plane,  $U_0$  is the initial amplitude, w is the frequency of oscillation and  $\delta$  is a spatial decay constant given by

$$\delta = \sqrt{\frac{i \omega \rho}{\eta}}$$
.

For the solutions of polyox being investigated the viscosity is always less than one poise, the frequency is greater than ten kHz and the density is approximately that of water. Thus a shear wave at a frequency of ten kHz is attenuated to a value of 1/e U<sub>0</sub> in approximately 0.006 centimeters from the surface of the rod. Since the shear wave is attenuated in such a small distance compared to the radius of the rods used (0.635 centimeters), the assumption of plane waves is justified in formulating a working equation. However it also makes it

necessary to measure the viscoelastic properties by observing the loading effect of the fluid on the rod rather than by direct measurements. The viscous force the fluid exerts on the rod is given from the basic definition of viscosity as

$$F_y = S \eta \left( \frac{\partial U_y}{\partial z} \right)_{z=0}$$

where S is the surface area in contact with the fluid. The specific acoustic impedance Z for shear waves is defined by

$$Z = \frac{F/s}{U_y}$$

which, upon making the substitutions and dropping the time dependence becomes

If R and X are the specific load resistance and reactance,  ${\bf Z}$  can be written as

$$Z = R + iX$$

Gemant (3) proposed that  $\gamma$  be written as

$$\eta^* = \eta_1 + i \eta_2$$

where  $\eta_i$  is the normal flow viscosity coefficient and  $\eta_2$  is an elastic viscosity term which vanishes for normal fluids. Substituting  $\eta^*$  for  $\eta$  gives

$$Z = R + i X = (\pi F \rho \eta^*)^{\frac{1}{2}} (1 + i).$$

Squaring and separating the real and imaginary parts gives

$$\eta_1 = \frac{2RX}{\omega R}$$

$$\eta_2 = \frac{R^2 - X^2}{\omega P}.$$

Thus if R and X can be measured,  $\eta_{\it l}$  and  $\eta_{\it 2}$  can be calculated.

For torsional waves propagating down radially symmetric rods the tangential particle displacement  $\Theta$  is given by

$$\theta = J_1(ka) \exp(i\omega t - \Gamma_2)$$

where

$$k^2 = \frac{\rho \omega^2}{A} + \int_{-\infty}^{\infty}$$

and  $\mathcal{M}$  is the shear modulus of the rod and the wave is traveling in the +z direction with a propagation constant

$$\Gamma = A + iB$$

where A is the attenuation in nepers per centimeter and B is the phase shift in radians per centimeter (8). The specific acoustic impedance at a radius a is given by

$$Z = \frac{-T_{re}}{\frac{\partial \Theta}{\partial t}} = \frac{M(\frac{\partial \Theta}{\partial r} - \frac{\Theta}{r})}{\frac{\partial \Theta}{\partial t}}$$

which becomes for this case,

$$Z = \frac{i / k}{\omega} \left[ \frac{J_0(ka)}{J_1(ka)} - \frac{2}{ka} \right].$$

Since by suitable choice of parameters the term ka can be kept small in the expansions of the Bessel functions the higher order terms may be neglected, giving

$$Z = \frac{i / a k^2}{4 \omega} .$$

Assuming that the loading of the rod without the fluid is zero, then k must be zero and

$$\Gamma^2 = -\frac{\rho \omega^2}{\pi} = (A_0 + i B)^2$$

For metals  $A_{\rm o}$  is very much smaller than  $B_{\rm o}$  and the terms  $2A_{\rm o}B_{\rm o}$  and  $A_{\rm o}^2$  are neglected. Thus

$$B_o = \omega \sqrt{\frac{\rho}{M}} = \frac{\omega}{V_o} ,$$

where Vo is the velocity of propagation of the wave in the rod.

Surrounding the rod with a fluid gives

$$k^2 = \frac{\rho \omega^2}{\rho} + \Gamma^2 = (A_0 + i B_0)^2 + (A + i B)^2$$
.

Since  $(B_O + B) >> (A_O + A)$  in the usual case this becomes

$$k^{2} = (B_{o} + B)(-\Delta B + i \Delta A) \doteq 2 B_{o} (-\Delta B + \epsilon \Delta A)$$

where  $\Delta$  B and  $\Delta$  A are (B - B<sub>O</sub>) and (A - A<sub>O</sub>).

Substituting, the impedance becomes

$$Z = \left(\frac{\rho V_{0} a}{2}\right) \left(\Delta A + i \Delta B\right),$$

but since the observed attenuation and phase change are due to the total length of wave travel, the observed changes must be divided by the length  $2nl_0$ , where n is the number of the echo used and  $l_0$  is the length of rod covered by the fluid. This gives

(1) 
$$Z = \left(\frac{\rho V_o}{4\pi}\right) \left(\frac{\partial}{\partial o}\right) \left(\Delta A' + \Delta B'\right)$$

where  $\triangle A^*$  and  $\triangle B^*$  are now the total change in the attenuation and the phase resulting from immersing the rod in the fluid. These are readily measurable quantities.

Instead of determining the complex viscosity, an alternate determination of the complex shear modulus G\* given by

$$G^* = G' + i G'' = \frac{m^*}{i \omega}$$

could be made.

#### 3. Measurements

The velocity of propagation of the wave in the rod was determined by measuring the frequency change necessary to give a phase change of 2 77 radians since

where l is the length of the rod, m is the integer number of  $2\pi$  radian shifts, and  $\theta$  is the phase change upon reflection (10). The number of phase shifts m is given by

$$m = \frac{f}{\Delta f_i}$$

where  $\Delta f_i$  is the frequency change required for a shift of 2  $\pi$  radians. The velocity of propagation can be determined from the slope of a plot of m as a function of frequency. The velocity  $V_0$  was found to be slightly different for each rod since the rods were made from different stock. This variation was less than 0.8 percent. The observed velocity for each rod was used for calculations involving that rod.

All rods were checked using Newtonian fluids in the expected viscosity range of the polyox solutions to determine if the fluids had the expected loading effect on the rod as given by equation (1). It was found that the loading of the fluid on the rod was consistantly within the experimental accuracy as long as the rods were highly polished. Since polyox solutions are basic, the use of aluminum rods prevented prolonged immersion in the polyox solutions. To avoid any increase in the loading due to the corrosion of the polished surface of the rods due to chemical reaction, the rods were repolished between successive runs and the time of submersion in the solutions was held to a minimum. The rods were also checked using standard fluids from time to time to insure that there was no degradation due to the repeated polishing.

It was not possible to measure with sufficient accuracy the loading effect of the fluids on the rods using the first returned echo. The echo train held the pulse shape until the fourth or greater echo so the third echo was used to give a greater attenuation accuracy.

The phase shift was measured by first calibrating the equipment in air to determine the frequency shift required to establish balance between successive  $2\pi$  radian shifts of phase. Then surrounding the rod with fluid, the frequency shift required to re-establish balance was measured and converted into the phase shift in radians by

$$\Delta B' = \frac{2\pi \Delta F}{\Delta F_i}$$

Temperature control of the test fluid and the aluminum rod is needed because both the fluid properties and the velocity in the rod are temperature dependent. The entire system was enclosed in a water jacket with the temperature controlled to within  $25.075 \pm .025$  °C.

The effect of this uncertainty on the velocity of the propagated wave pulse is 150 centimeters per second or 0.05 percent of the velocity. The effect on the phase of the wave pulse is 0.0056 radians or eight percent of the smallest observed phase shift.

The effect on the fluid properties is estimated to be less than 0.09 percent.

# 4. Equipment and Procedures

#### (a) Details of equipment

Following a method described by McSkimin (11), the equipment was constructed in the following manner.

The torsional transducers were made from one half inch barium titanate cylinders. Polarizing electrodes were placed as shown in Figure 2 and the crystals then heated in an oil bath to above the Curie temperature and 10,000 volts DC applied. After applying the voltage the crystal temperature was returned to room temperature with the voltage applied. Driving electrodes were then painted on the crystal using silver conducting paint as shown in Figure 2 (5). The

crystal frequency was then checked against computed values. This check also allowed a verification that only the torsional mode would be excited.

The rods were cut from standard one half inch aluminum bar stock and polished in a lathe using 600A sand paper followed by the use of automotive rubbing compound until a high polish was obtained. The crystals were then cemented to the rods using epoxy cement to give a hard connection.

For measurements the rods were supported inside the water jacket by needle pivot bearings at the top and bottom. The water jacket had an inside diameter of 3.3 centimeters. This distance is sufficient to prevent any wall effects. The water jacket was open at both ends to facilitate the insertion of the rod and the cleaning of the jacket between runs. The bottom was sealed with a plug containing the pivot bearing and a filling pipe. The top pivot bearing was held by an aluminum plate mounted by screws to nuts cemented to the jacket. A copper-constantan thermocouple, mounted in a thin wall copper tube, was inserted into the water jacket for measurement of the temperature inside the inner bore of the water jacket. The thermocouple was capable of measuring a temperature change of 0.025 °C and it was found that the temperature after equilibrium was established did not vary a measurable amount.

A block diagram of the equipment setup used for measurements is shown in Figure 1. The signal from the oscillator was split into two channels to provide a driving signal to the crystal and a direct reference signal for phase and echo amplitude measurements. The driving signal was pulsed by the toneburst generator giving a pulse of eight

or 12 cycles depending upon the frequency used. A second gate circuit triggered by the toneburst generator, was added to give additional isolation. The toneburst generator and gate combination gave -76 db isolation for the ratio of the cut off signal to the continuous signal. The pulse repetition rate of the toneburst generator was set at about two pulses per second, which allowed sufficient time for each echo train to be absorbed to below the noise level. The return echos were then amplified and mixed with the direct, attenuated signal from the oscillator. This signal was then observed on an oscilloscope triggered by the toneburst generator.

The direct reference signal was attenuated by a 600 ohm noninductive attenuator capable of measuring 0.1 db steps. Frequency was measured using a counter with a ten second count period.

All electronic equipment was operated using constant voltage generators. This was found necessary to give stable operation of the oscillator and to reduce the noise in the amplifier and toneburst generator. The oscillator was left in continuous operation with no load between measurements to insure minimum frequency shift due to thermal instability in the oscillator. The other equipment was turned on at least one hour prior to making measurements.

#### (b) Procedures

For changes in attenuation and phase, the mixed signal was displayed on the oscilloscope set on time and magnitude scales to give as large a display of the third echo as possible. With only air surrounding the rod, eight measurements of frequency and attenuation necessary to cancel the echo were made, from which an average value was obtained. The frequency shift required to give 2 77 radian phase

shift from each frequency reading was recorded. The temperature of the rod was measured and recorded. The preheated fluid was then forced into the inner bore of the water jacket using compressed air. This was found to be necessary as filling from the top created air bubbles which required a considerable time period to settle out. To avoid the possibility of the temperature not being constant across the tube, the thermocouple was arranged so that it could be placed next to the rod prior to a run and then shifted away from the rod during the acoustic measurements. When thermal equilibrium was reached, the measurements of frequency and attenuation to give echo cancellation were repeated. The change in frequency and attenuation were converted into changes of phase in radians and attenuation in nepers. Using these values of changes, the resistive and reactive loading could then be computed. At least two seperate measurements using different fluids of the same concentration were made and these measurements averaged to give the final value of acoustic loading due to the fluid.

The smooth curves of the acoustic loading were then used to obtain values of resistance and reactive loading to be used in computing the terms of the complex viscosity and shear modulus.

# (c) Solution mixing procedure

The solutions were mixed using a low speed variable speed mixer with a maximum speed of 200 rpm. The speed of the mixer and the depth of the blade of the mixer were adjusted to give the water a vortex not quite touching the blade of the mixer. The polyox powder was then added with a shaker until the surface was saturated with powder. This was repeated as the polyox was drawn under the surface

by the vortex. By using this technique, large lumps of undissolved polyox could be avoided. After all the polyox was added to the water, the solution was allowed to mix until there were no particles of undissolved polyox suspended in the solution. The adding of the polyox and dissolving after all had been added took from several hours to two days, depending upon the concentration.

#### 5. Results

The frequency range covered in the present study is too narrow to describe adequately the viscoelastic behavior of the polyox solutions as a function of frequency. However, when the present results are combined with the results obtained in a previous study by Kinnier (4), it is possible to get some measure of the frequency response. Figures 7 and 8 show the frequency response of the real parts of the complex viscosity and shear modulus.

The behavior of the real part of the complex shear modulus is very similar to that found by Mason (8) for solutions of polyiso-butylene at higher frequencies. Since polyox is a longer molecule, the lower frequency was expected. Mason gave the interpretation of the steep rise if G' as the relaxation of the smallest chain segment. This interpretation seems to apply for polyox as it is the first relaxation that would involve all molecules since it does not depend upon the concentration or the length of the molecule. Below the frequency of this relaxation, G' decreases slowly as frequency decreases. Philippoff (6) describes this as the behavior of a fluid with a distribution of relaxation times. Since polyox molecules have a distribution of molecule lengths, it was expected that the relaxations dependent upon the length of the polyox molecule would also have a

distribution of frequencies.

The real part of the complex viscosity was found in this study to approach a steady value at the higher frequencies. Since the 0.25 and 0.50 percent solutions approached the same limiting value of 0.015 poises and the one percent solution approaches a higher value of 0.023 poises, the idea introduced by Peterlin and Signer (6) of a "local viscosity" which depends upon the interaction of the molecules with each other appears to hold for the polyox solutions.

#### 6. Discussion of Error

Statistical uncertainty in the observed quantities ranged from a high of 17 percent to five percent. The higher values were for the measurements in the lower frequencies and lower concentrations. Smoothing of the observed data was accomplished by plotting the resistive and reactive loading versus frequency and taking the best fit of these points to compute the components of the complex viscosity and complex shear modulus. Thus the probably error is less than the statistical error and this can be observed in the smoothness of the transition from values observed in this study to the values found by Kinnier and Reister.

## 7. Acknowledgements

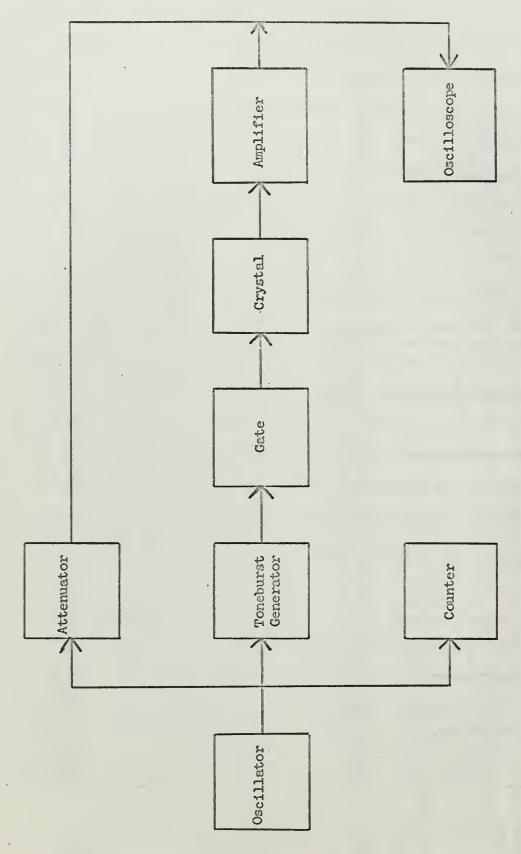
This research was conducted at the United States Naval Postgraduate School, Monterey, California. The writer wishes to express his appreciation for the intellectual and moral support given him by Professor O. B. Wilson, Jr. Support was provided in part by the Office of Naval Research and the Bureau of Ships.

Frequency (cps)	201,44	44	30365	15	40268	99	50509	60	60655	5	70151	
conc.	R	×	R	×	R	×	R	×	R	×	M	×
.25	33.5		40.9	39.1	9.94	31.9 40.9 39.1 46.6 44.1 51.1 47.5 55.2 50.3 58.9 52.5	51.1	47.5	55.2	50.3	58.9	52.5
• • 5	35.2	32.3	41.6	39.0	47.5	32.3 41.6 39.0 47.5 40.0 54.5 40.5 61.5 43.0 67.3 45.2	54.5	140.5	61.5	43.0	67.3	45.2
1.0	49.7	34.8	57.1	42.9	65.9	34.8 57.1 42.9 62.9 49.3 68.3 54.5 74.0 59.0 81.0 63.1	68.3	74.5	74.0	59.0	81.0	63.1

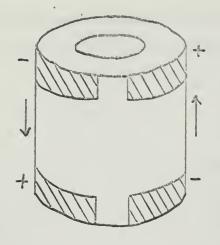
Observed Velues of the Resistive and Reactive Loading. The Resistive and Reactive Loading are in Dync-sec/cm² and the Concentration in Weight Percent. Table 1.

requency (cps)	20144	7	30365	55	40268	80	50509	0	60655	5	70151	51
conc.	ů.	g g g	<b>5</b>	50	Ç,	G. 1	G	9 40	ď	G. t	Ğ	G
.25	0110	21,30	260	2110	130	3950	250	4.730	610	5/180	720	6200
.5	961	2280	210	3251	657	5807	1333	4423	1937	5290	2491.	9609
1.0	1272	3466	1445	4918	1539	6892	1695	94147	2014	8761.	2603	10,255

Real and Imaginary Components of the Complex Shear Modulus. G' and G'' are in Dynes/cm2 and Concentration in Weight Percent. Table 2.



Block Diagram Showing Experimental Setup for Measurements Using Traveling Torsional Waves. Figure 1.



(a)

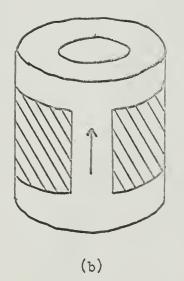
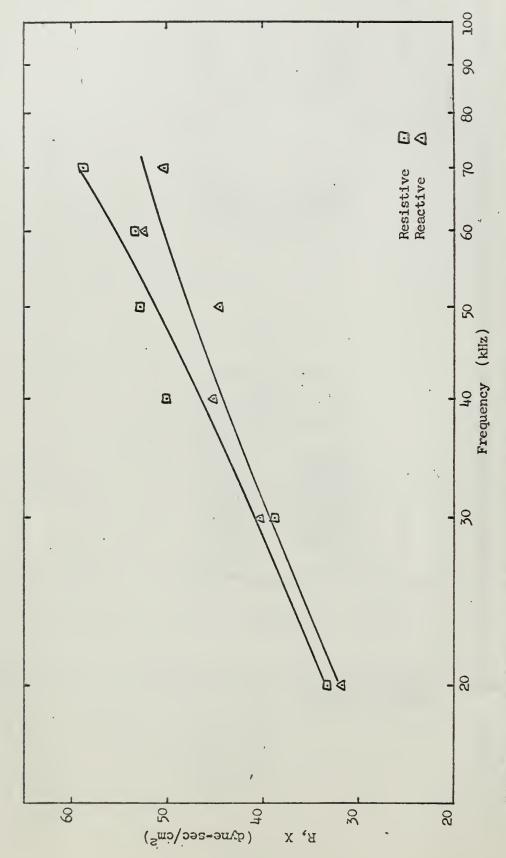
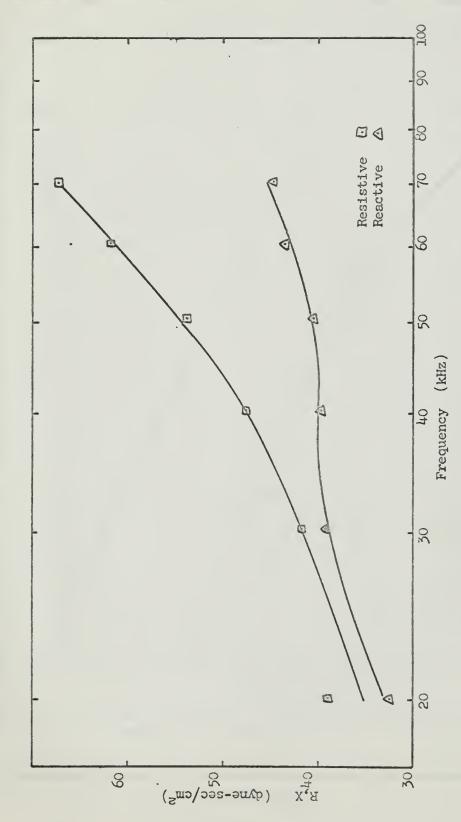


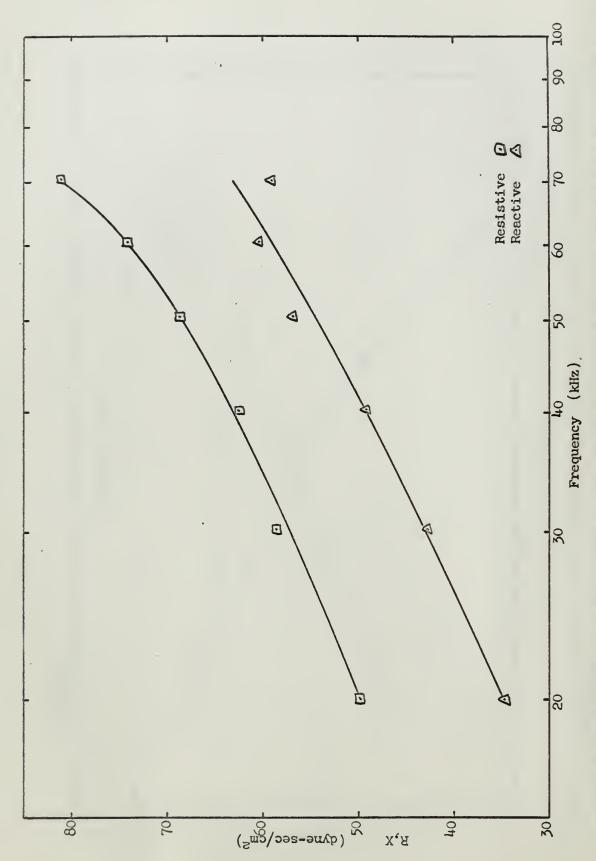
Figure 2. Barium Titanate Crystal Electrode Location for (a) Polarization and (b) Driving.



The Resistive and Reactive Loading for 0.25 Percent Polyethylene Oxide as a Function of Frequency. Figure 5.



The Resistive and Reactive Loading for 0.5 Percent Polyethylene Oxide as a Function of Frequency Figure 4.



The Resistive and Reactive Loading for One Percent Polyethylene Oxide as a Function of Frequency. Figure 5.

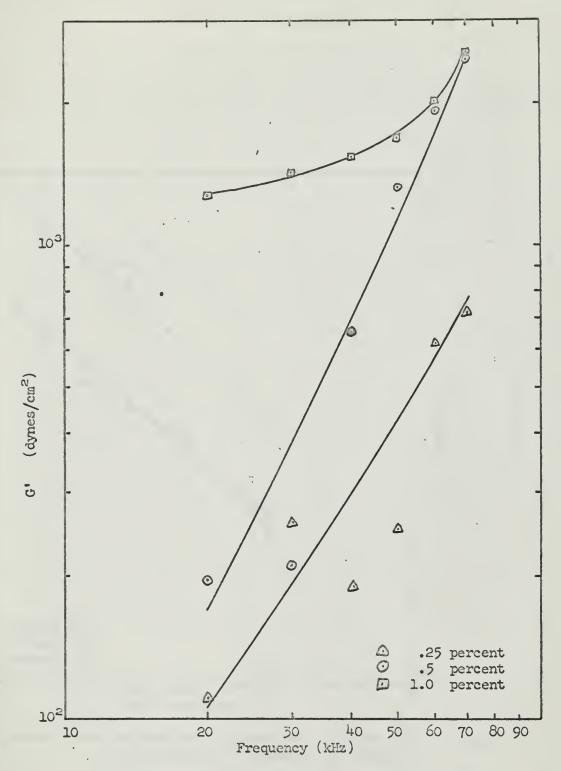


Figure 6. The Real Component of the Complex Shear Modulus as a Function of Frequency and Concentration.

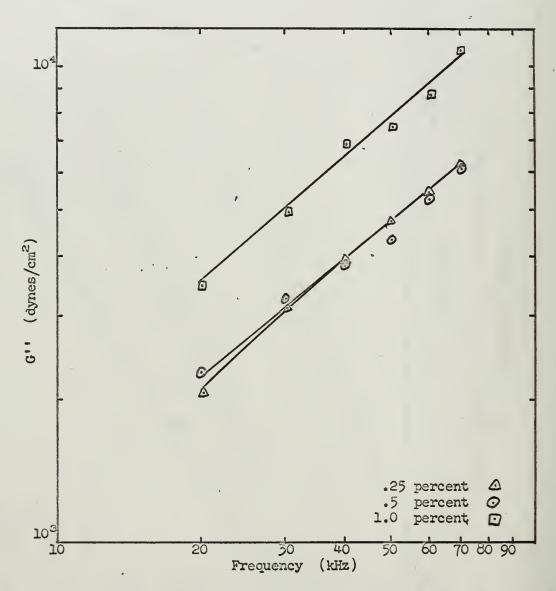


Figure 7. The Imaginary Component of the Complex Shear Modulus as a Function of Frequency and Concentration.

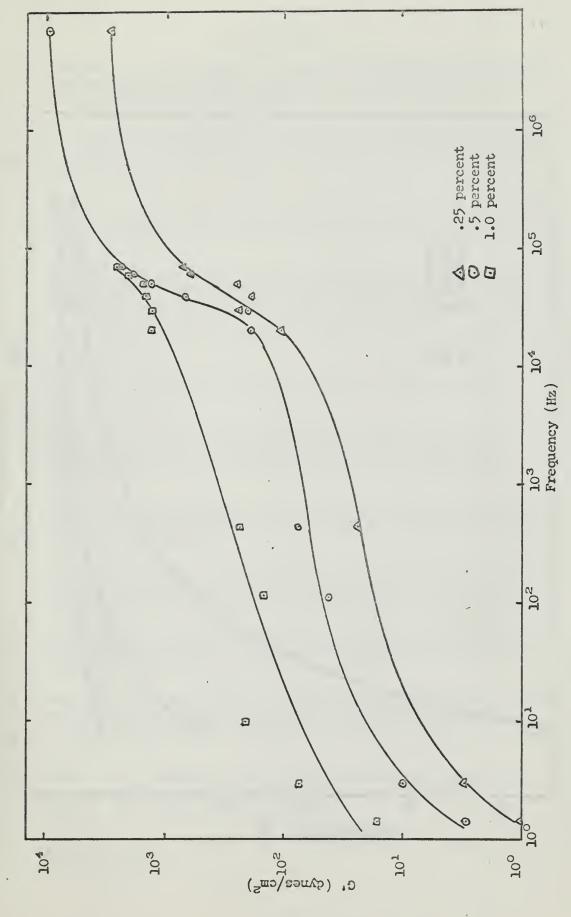
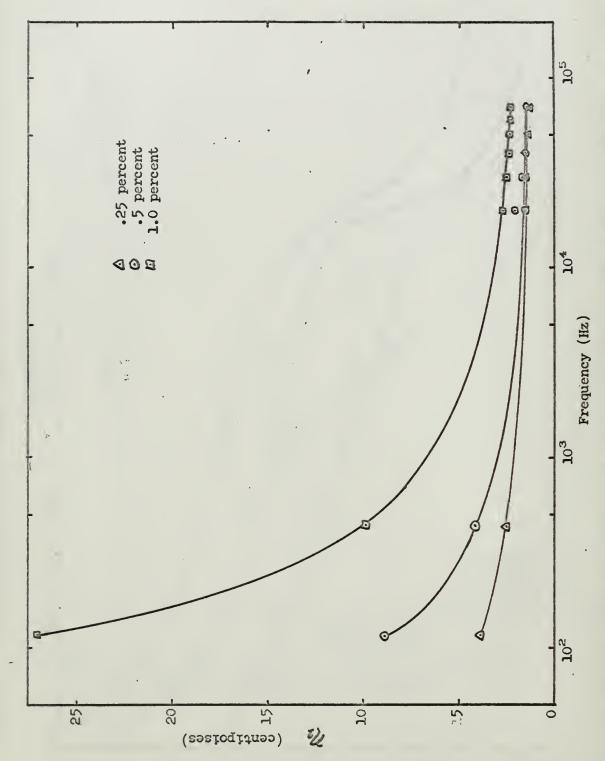


Figure 8. The Real Component of the Complex Shear Modulus as a Function of Frequency and Concentration.



The Real Component of the Complex Viscosity as a Function of Frequency and Concentration. Figure 9.

#### BIBLIOGRAPHY

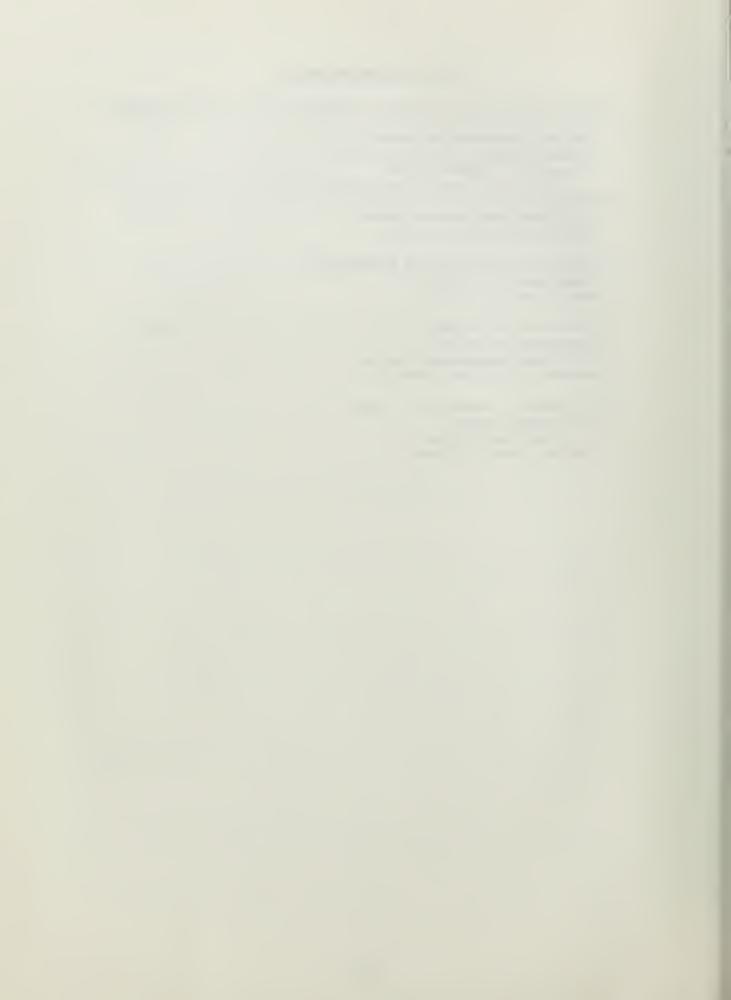
- Chester, S.A., Measurement of Viscoelastic Properties of Dilute Aqueous Polyethylene Oxide Using Acoustic Methods, Thesis, U.S. Naval Postgraduate School, 1964.
- 2. Barlow, A.J., Harrison, G., Richter, J., Seguin, H., and Lamb, J., Electrical Methods for the Viscoelastic Behavior of Liquids Under Cyclic Shearing Stress, Laboratory Practice, November, 1961, 786-801.
- 3. Gemant, A., The Conception of a Complex Viscosity and Its Application to Dielectrics, Transactions of the Faraday Society, v. 31, 1935, 1582-1590.
- 4. Kinnier, J.W. and Reister, W.A., Investigation of the Low Frequency Dynamic Viscoelastic Properties of Aqueous Polyethylene Oxide Solutions, Thesis, U.S. Naval Postgraduate School, 1965.
- 5. Mason, W.P., Physical Acoustics, Volume I, Part A, Academic Press, 1964.
- 6. Mason, W.P., Physical Acoustics, Volume II, Parts A and B, Academic Press, 1965.
- 7. Mason, W.P., Baker, W.O., McSkimin, H.J., and Heiss, J.H., Measurement of Shear Elasticity and Viscosity of Liquids at Ultrasonic Frequencies, Physical Review, v.75, March, 1949, 936-946.
- 8. Mason, W.P., and McSkimin, H.J., Mechanical Properties of Polymers at Ultrasonic Frequencies, The Bell System Technical Journal, January, 1952, 122-171
- 9. Mason, W.P., Baker, W.O., McSkimin, H.J., and Heiss, J.H., Mechanical Properties of Long Chain Molecule Liquids at Ultrasonic Frequencies, Physical Review, V. 73, May, 1948, 1074-1091.
- 10. McSkimin, H.J., Ultrasonic Measurement Techniques Applicable to Small Solid Specimens, Journal of the Acoustical Society of America, √. 22, July, 1950, 413
- 11. McSkimin, H.J., Measurement of Dynamic Shear Viscosity and Stiffness of Viscous Liquids by Means of Traveling Torsional Waves, Journal of the Acoustical Society of America, v. 24, July, 1952, 355-365.
- 12. Rouse, P.E., A Theory of the Linear Viscoelastic Properties of Dilute Solutions of Coiling Polymers, Journal of Chemical Physics, v. 21, July, 1953, 1272-1280.
- 13. Schlichting, H., Boundary Layer Theory, McGraw-Hill Book Company, Inc., 1960

#### BIBLIOGRAPHY

- 14. Union Carbide Chemical Company, "Polyox" Water Soluable Resins, January, 1964, Advance Technical Information Bulletin f-40246-C.
- 15. Vohr, J.C., Thesis, U.S. Naval Postgraduate School, 1966
- 16. Williams, M.C., Normal Stresses and Related Viscoelastic Phenomena in Polymer Solutions, Thesis, University of Wisconsin, 1964

# INITIAL DISTRIBUTION LIST

		No.	Copies
1.	Defense Documentation Center Cameron Station Alexandria, Virginia 22314		20
2.	Library U.S. Naval Postgraduate School Monterey, California 93940		2
3.	Ordnance Systems Command Headquarters Department of the Navy Washington, D.C. 20360		1
4.	Professor O.B. Wilson, Jr. Department of Physics U.S. Naval Postgraduate School Monterey, California 93940		12
5.	LT Robert J. Prather, Jr., USN USS TOPEKA (CLG-8) c/o Fleet Post Office San Francisco, California		1



#### Security Classification

(Security clessification of title, body of a	OCUMENT CONTROL DATA - R		the overall report is clessified)
1. ORIGINATING ACTIVITY (Corporate author)			ORT SECURITY CLASSIFICATION
U.S. Naval Postgraduate	School	UN	NCLASSIFIED
Monterey, California 939	40	26 GROU	JP
3. REPORT TITLE INVESTIGATION OF THE ULT AQUEOUS POLYETHYLENE OXI		STIC PRO	PERTIES OF
4. DESCRIPTIVE NOTES (Type of report and inc Thesis, M.S., May 1966	clusive dates)		
PRATHER, Robert J., Jr.,	LT, USN		
6. REPORT DATE May 1966	70. TOTAL NO. OF	PAGES	75. NO. OF REFS
Sa. CONTRACT OR GRANT NO.	90. ORIGINATOR'S	REPORT NUI	
b. PROJECT NO.			
c.	Sb. OTHER REPORT	NO(S) (An)	other numbers that may be assigned
d.			
10. AVAIL ABILITY/LIMITATION NOTICES	busin copies of this w	ереть в	
11. SUPPLEMENTARY NOTES	12. SPONSORING MII Ordnance S Navy Depar	ystems C tment	ommand Headquarters

#### 13. ABSTRACT

Some of the viscoelastic properties of aqueous solutions of polyethylene oxide were studied using the method of pulsed torsional wave propagation in the ultrasonic frequency range. Measurements of the changes in attenuation and phase of the wave train in a rod when the rod is immersed in the solutions permit calculation of the components of the complex shear modulus (or the complex viscosity). The results from this study are combined with those of others at different frequencies to obtain a measure of the variation of the viscoelastic properties over a wide frequency range. This can be interpreted qualitatively in terms of a distribution of relaxations at low frequencies corresponding to the configurational relaxation of the molecule as a whole and a relaxation frequency of approximately 40 kHz corresponding to that of the shortest chain segment. The real part of the complex viscosity approaches a value at high frequencies, dependent upon the concentration, which is greater than that of water thus showing the existance of a "local viscosity" which is dependent upon concentration. (U)

DD . FORM 1473

UNCLASSIFIED
Security Classification

Security Classification

14.	VPV WARRA		LIN	KA	LIN	KB	LIN	KC
	KEY WORDS		ROLE	WT	ROLE	WT	ROLE	WT
	Polyethylene Oxide Non-Newtonian Fluid Viscoelastic Fluid			-				
							17.0	
		-		-	-			

#### INSTRUCTIONS

- 1. ORIGINATING ACTIVITY: Enter the name and address of the comtractor, subcontractor, grantee, Department of Defense activity or other organization (corporate author) issuing the report.
- 2a. REPORT SECURITY CLASSIFICATION: Enter the overall security classification of the report. Indicate whether "Reatricted Data" is included. Marking is to be in accordance with appropriate security regulations.
- 2b. GROUP: Automatic downgrading is specified in DoD Directive 5200.10 and Armed Forces Industrial Manual. Enter the group number. Also, when applicable, show that optional markings have been used for Group 3 and Group 4 as authorized.
- 3. REPORT TITLE: Enter the complete report title in all capital letters. Titles in all cases should be unclassified. If a meaningful title cannot be selected without classification, ahow title classification in all capitals in parenthesis immediately following the title.
- 4. DESCRIPTIVE NOTES: If appropriate, enter the type of report, e.g., interim, progress, summary, annual, or final. Give the inclusive dates when a specific reporting period is covered.
- 5. AUTHOR(S): Enter the name(s) of author(s) as shown on or in the report. Enter last name, first name, middle initial. If military, show rank and branch of service. The name of the principal author is an absolute minimum requirement.
- 6. REPORT DATE: Enter the date of the report as day, month, year, or month, year. If more than one date appears on the report, use date of publication.
- 7a. TOTAL NUMBER OF PAGES: The total page count ahould follow normal pagination procedures, i.e., enter the number of pagea containing information.
- 7b. NUMBER OF REFERENCES: Enter the total number of references cited in the report.
- 8. CONTRACT OR GRANT NUMBER: If appropriate, enter the applicable number of the contract or grant under which the report was written.
- 8b, 8c, & 8d. PROJECT NUMBER: Enter the appropriate military department identification, such as project number, aubproject number, system numbers, task number, etc.
- 9a. ORIGINATOR'S REPORT NUMBER(S): Enter the official report number by which the document will be identified and controlled by the originating activity. This number must be unique to this report.
- 9b. OTHER REPORT NUMBER(S): If the report has been assigned any other report numbers (either by the originator or by the sponsor), also enter this number(s).
- 10. AVAILABILITY/LIMITATION NOTICES: Enter any limitations on further dissemination of the report, other than those

imposed by security classification, using standard statements such as:

- (1) ''Qualified requesters may obtain copies of this report from DDC.''
- (2) "Foreign announcement and dissemination of this report by DDC is not authorized."
- (3) "U. S. Government agencies may obtain copies of this report directly from DDC. Other qualified DDC users shall request through
- (4) "U. S. military agencies may obtain copies of this report directly from DDC. Other qualified users shall request through
- (5) "All distribution of this report is controlled. Qualified DDC users shall request through

If the report has been furnished to the Office of Technical Services, Department of Commerce, for sale to the public, indicate this fact and enter the price, if known

- 11. SUPPLEMENTARY NOTES: Use for additional explanatory notes.
- 12. SPONSORING MILITARY ACTIVITY: Enter the name of the departmental project office or laboratory sponsoring (paying for) the research and development. Include address.
- 13. ABSTRACT: Enter an abstract giving a brief and factual summary of the document indicative of the report, even though it may also appear elsewhere in the body of the technical report. If additional space is required, a continuation sheet shall be attached.

It is highly desirable that the abstract of classified reports be unclassified. Each paragraph of the abstract shall end with an indication of the military security classification of the information in the paragraph, represented as (TS), (S), (C), or (U).

There is no limitation on the length of the abstract. However, the suggested length is from 150 to 225 words.

14. KEY WORDS: Key words are technically meaningful terms or short phrases that characterize a report and may be used as index entries for cataloging the report. Key words must be selected so that no security classification is required. Identifiers, such as equipment model designation, trade name, military project code name, geographic location, may be used as key words but will be followed by an indication of technical context. The assignment of links, rules, and weights is optional.

DD FORM 1473 (BACK)

UNCLASSIFIED







thesP83
Investigation of the ultrasonic dynamic

3 2768 001 93177 7
DUDLEY KNOX LIBRARY